



**INSTITUTE FOR SOCIAL RESEARCH • SURVEY RESEARCH CENTER**  
**SURVEY RESEARCH OPERATIONS**  
UNIVERSITY OF MICHIGAN

# Lunch & Learn: Survey Weights

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Paul Schulz



# Overview

- Part 1: What is a survey weight?
- Part 2: Components of survey weights
- Part 3: Examples



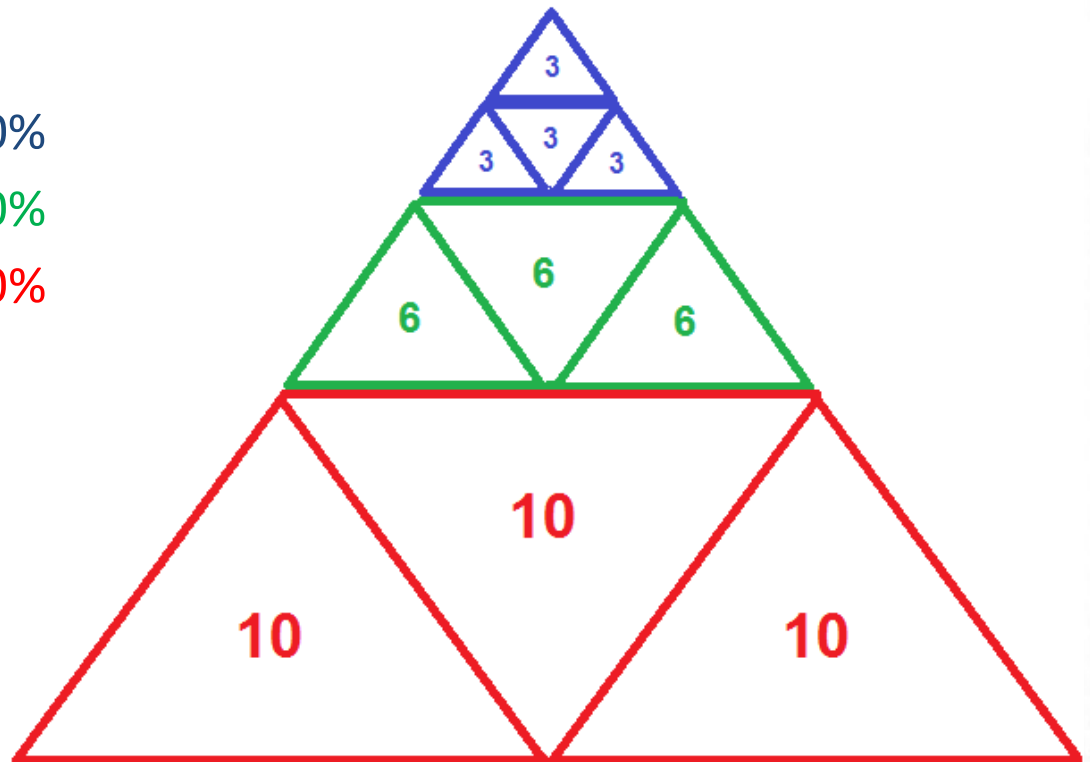
# PART 1: What is a survey weight?

- Weight = The number of additional elements represented by each sampled element.
- Used to make statistical estimates more representative of the whole population, by adjusting for sample design and nonresponse.
- A value assigned to each case in a data file.
- Example: a weight of 10 means this element represents itself and 9 other elements in the population.

# Toy Example: Pyramid Population

Blue area:  $12/60 = 20\%$   
Green area:  $18/60 = 30\%$   
Red area:  $30/60 = 50\%$

Total Size = 60



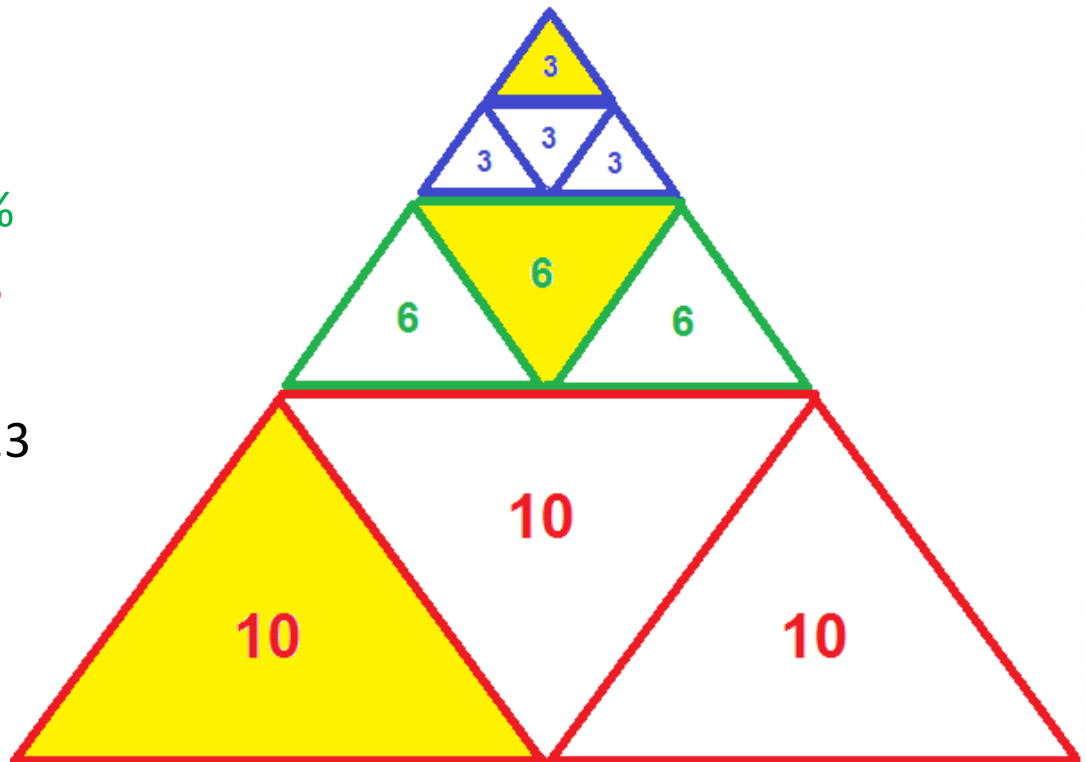
# Unweighted Estimates

Blue area:  $3/19=15.7\%$

Green area:  $6/19=31.6\%$

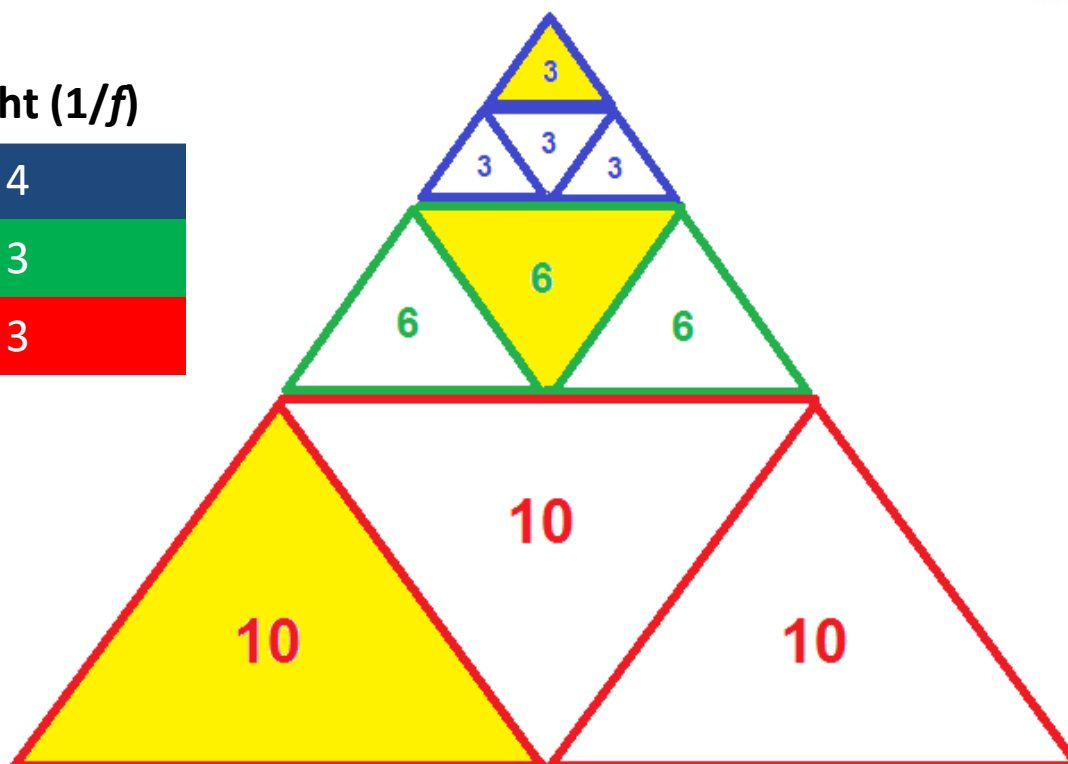
Red area:  $10/19=52.6\%$

Total Size:  $19 \times (10/3) = 63.3$



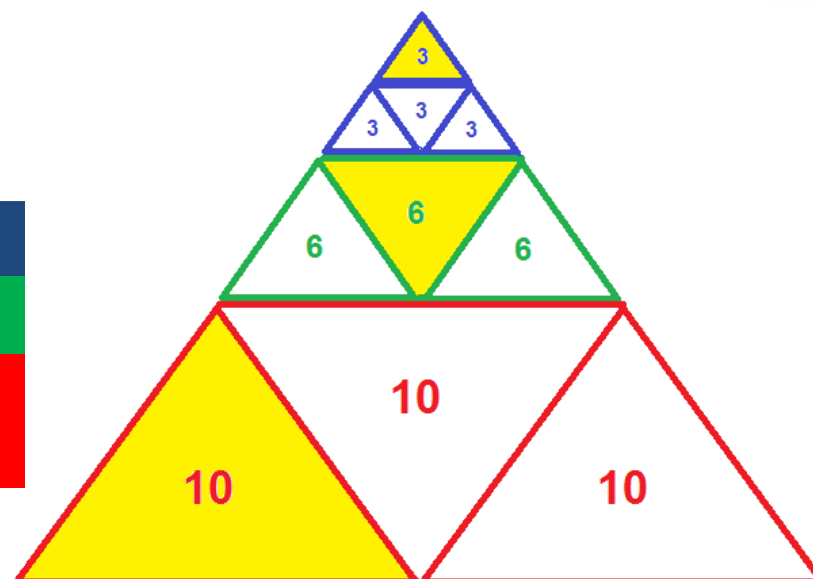
# Constructing Weights

Sampling fraction ( $f$ )	Weight ( $1/f$ )
$1/4$	4
$1/3$	3
$1/3$	3



# Weighted Estimates

	Unweighted Estimate	Weighted Estimate
% Area	15.7%	$(3*4)/60=20\%$
%Area	31.6%	$(6*3)/60=30\%$
% Area	52.6%	$(10*3)/60=50\%$
TOTAL	63.3	$3(4)+6(3)+10(3)=60$





# Weights in Data File

Obs. #	Measured Size	Weight
1	3	4
2	6	3
3	10	3



# PART 2: Components of a Survey Weight

1. Design Weights ( $D_i$ )
2. Nonresponse Adjustment ( $NR_i$ )
3. Calibration Adjustment ( $C_i$ )

$$\text{Total Weight } (W_i) = D_i * NR_i * C_i$$



# Component 1: Design Weights

- Also known as base weight.
- “Reverse” effects of sample design.
- Design Weight =  $1/(\text{selection probability})$
- Given perfect sample frame and no non-response, design weights alone could produce sufficient estimates.

## Component 2: Nonresponse Adj.

- When nonresponse is not random, nonresponse adjustment will reduce bias.
- Nonresponse adjustment =  $1/(\text{Prob. of Resp.})$
- Typically nonresponse is modelled using logistic regression (“propensity model”)
- Tradeoff between reducing bias and introducing variance.

# Component 3: Calibration Weight

- Calibration is used to create consistency between weighted estimates and external data source (pop. total, etc)
- Post-stratification weight is used to scale data to match known population totals across dimensions of interest.
- Requires external data source (e.g. Census) with a value for each cell of crossed variables of interest.



# Post-stratification Example

Gender	Sample %	Pop. %	Pop./Sample	P-S Weight
Male	.40	.50	.50/.40	1.25
Female	.60	.50	.50/.60	.833



# Post-stratification Example 2

P-S Weight = Pop. %/Samp. %	Age 18-30 (33%)	Age 31-55 (33%)	Age 55+ (33%)
Male (50%)	$.167/.12 = 1.39$	$.167/.10 = 1.67$	$.167/.18 = .93$
Female (50%)	$.167/.20 = .835$	$.167/.25 = .668$	$.167/.15 = 1.11$

# Other Techniques

- Raking – similar to post-stratification; iterative process used when only marginal totals are known.
- Trimming – Limit placed on the size of the weight to reduce variance, but introduces bias.



# Part 3: Practical Examples

1. STARRS AAS
2. Double-sample Adjustment





# Example 1: STARRS AAS

Sample: Stratified PPS sample of Army units by Army command (Forces Command, European command) with oversample of Special Operations command. Census of Soldiers within each selected unit.

Design weight: Unit-level  $1/(\text{Prob. Of Sel.})$

NR adjustment: Unit Size/# Responses

Calibration: Post-stratified to known Army totals within command.

## Example 2: Double-Sample

Sample: Existing project +  $\frac{1}{2}$  sample of NR units

Design weight:  $1/(\text{original prob. of selection})$

Double samp. adj.:

- 1 for responding units

- 0 for for non-selected NR units

- 2 for selected NR units.

NR adj. and calibration as needed.